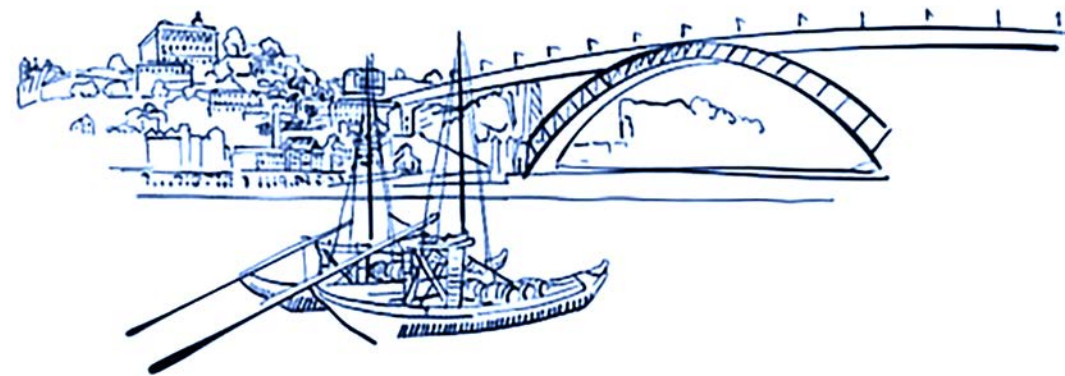




# Route-Aware Edge Bundling for Visualizing Origin-Destination Trails in Urban Traffic

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2. The Hong Kong University of Science and Technology
3. University of Groningen



## ■ Introduction

- OD Trails in Urban Traffic
- Prior Edge Bundling Methods
- Limitations of KDEEB

## ■ Route-Aware Edge Bundling

- Preprocessing:
  - map matching → hierarchical route structure construction → trail abstraction
- Bundling
  - optimal kernel size setting → density map generation
- Evaluation
  - Bundle termination
  - Bundle deviation

## ■ Conclusion and Future Work

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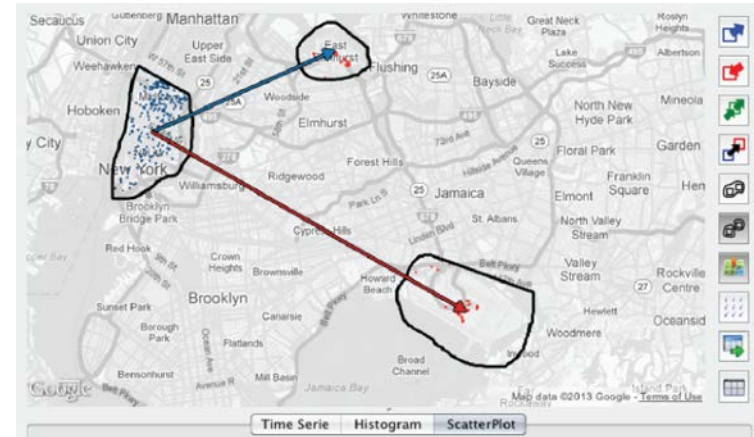
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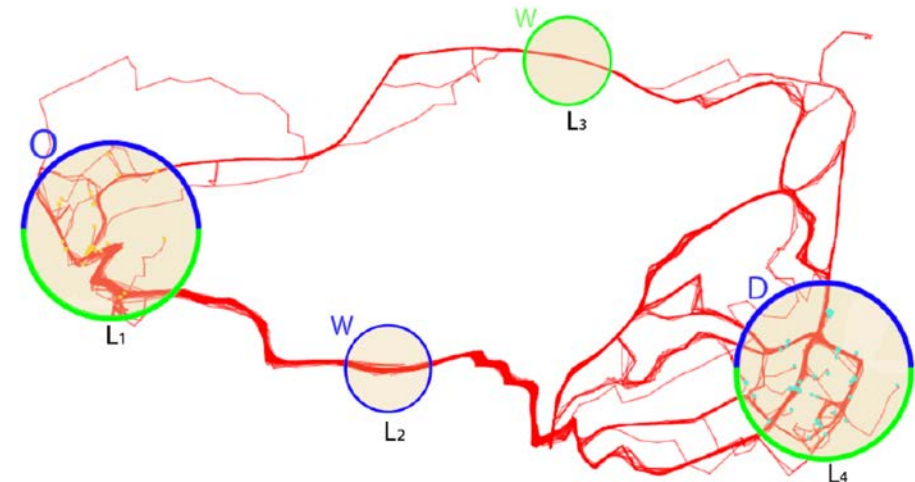
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# OD Trails in Urban Traffic

- Urban traffic data, e.g.,
  - Taxi trips in New York, Beijing, Shenzhen
  - Public transportation data in Singapore
  - Electric scooter tracks in Stuttgart
- Origin-destination (OD) is a fundamental concept in transportation, summarizing (people/vehicle/good) movements across geographic locations.
- Properties of OD trails in urban traffic
  - Locations
  - Times
  - Road network
  - Multi-modes



[Ferreira et al. 2013]

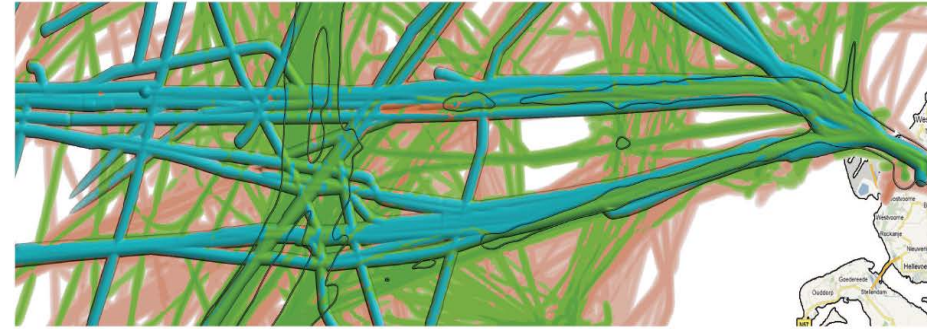


[Krüger et al., 2013]

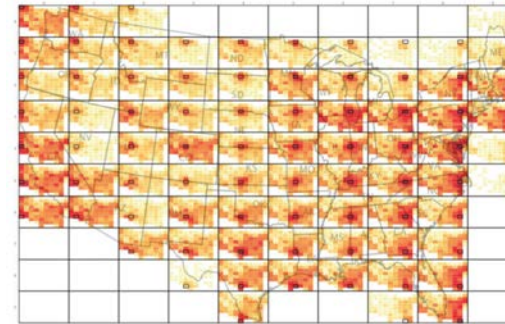


# OD Trail Visualization

- Density Map
  - Summarize trajectories and overview distribution.
- Spatial Aggregation
  - Partition underlying territory into appropriate areas.
- Map Matching
  - Align position records with road network data.
- Direct depiction
  - Directly plot trajectories into 2D/3D displays.



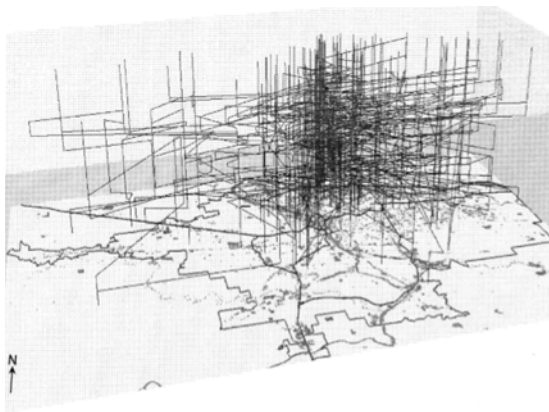
[Scheepens et al., 2011]



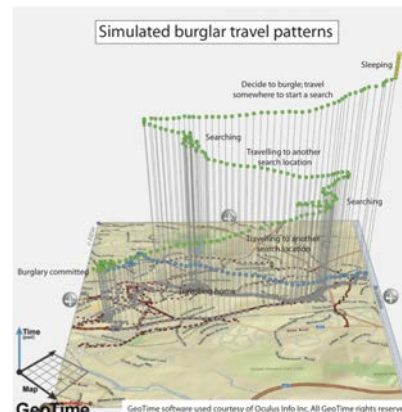
[Wood et al., 2010]



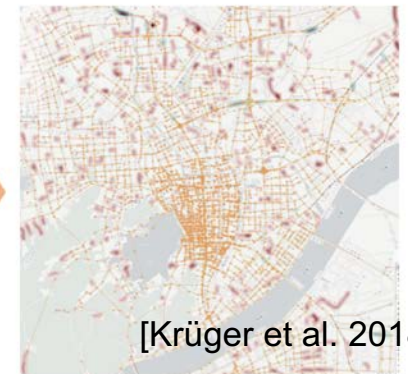
[Andrienko and Andrienko, 2011]



[Kwan, 2000]



[Kapler and Wright, 2004]



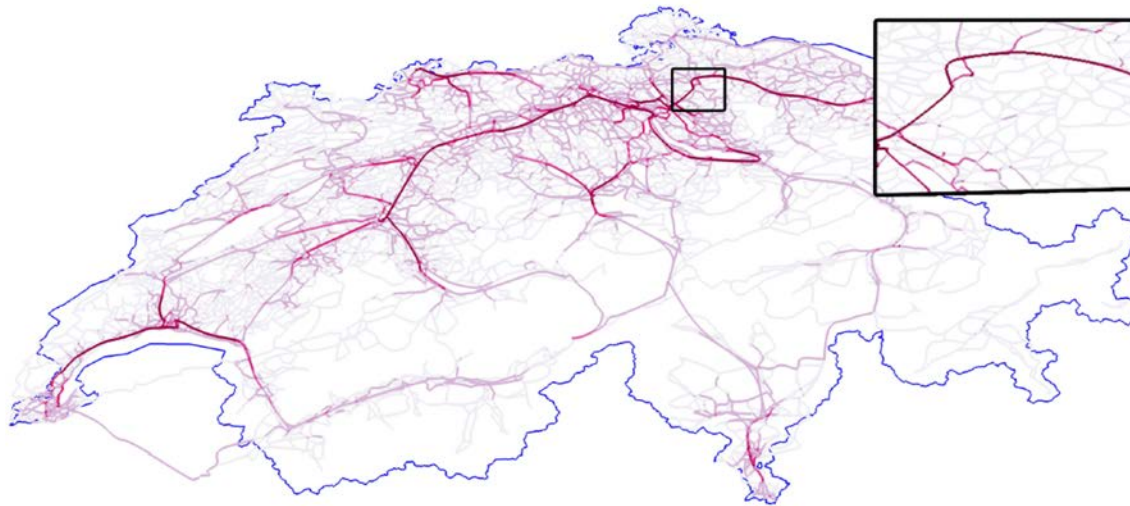
[Krüger et al. 2018]

# Prior Edge Bundling Methods

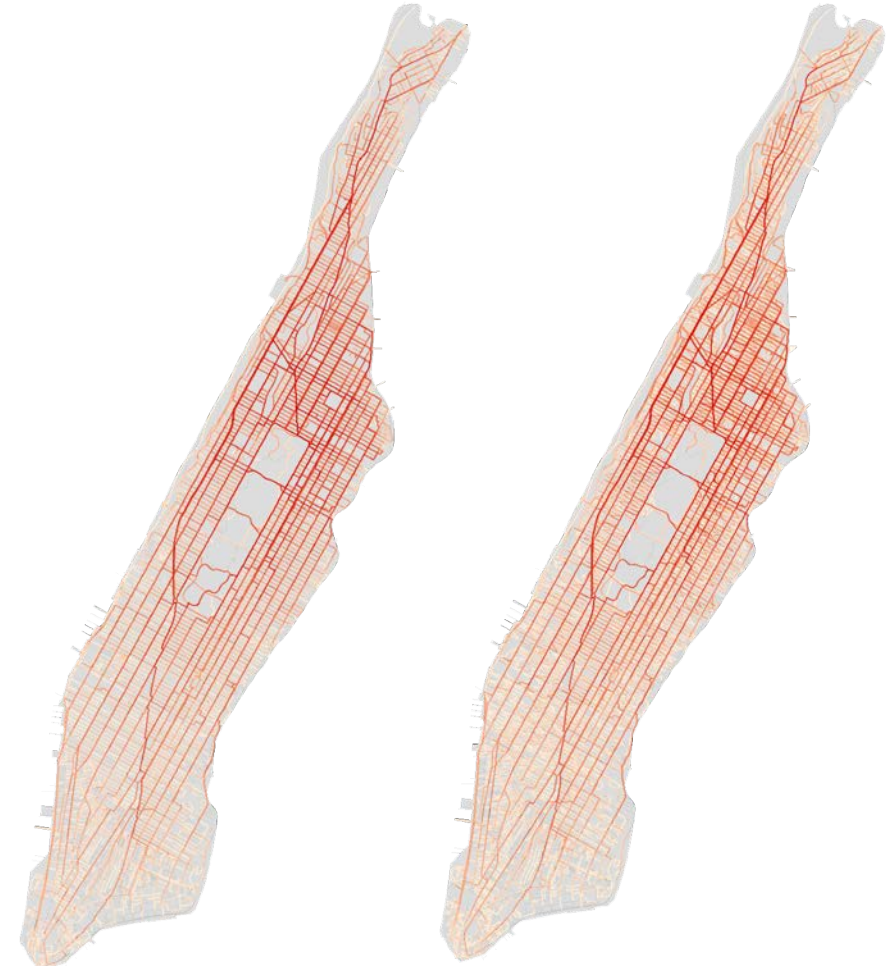
- *Geometry-based* methods: Use control mesh to specify how similar edges are routed.
  - Pros: Flexible to make control mesh
  - Cons: Constructing control mesh can be (very) slow
- *Force-based* methods: Model interaction between spatially close trails as a force field.
  - Pros: No need to make external control mesh
  - Cons: Slow – cannot handle a few thousands trails at interactive rates
- *Image-based* methods: Employ image-processing methods to accelerate the bundling process.
  - Pros: Feasible for GPU implementation – can process millions of trials at interactive rates.
  - Cons: No consideration of spatial constraints when applied to OD trails.

# Prior Edge Bundling Methods

- *Constrained Bundling*: Specific constraints are considered.
  - Ambiguity
  - 3D curved surfaces
  - Directions
  - Obstacles avoidance
  - **Vector map**



Vector map for Swiss commuter data  
[Thöny & Pajarola, 2015]



Map matching

Vector map

# Kernel Density Estimation Edge Bundling (KDEEB)

- We chose KDEEB for the basis of our method:
  - Fast in speed, meanwhile simple enough to implement
  - Be able to incorporate specific constraints

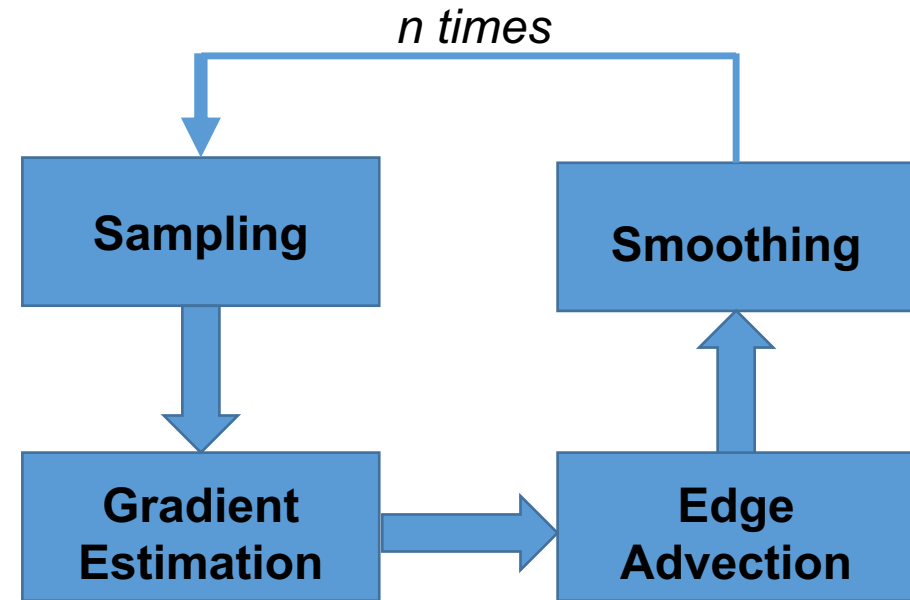
- KDEEB pipeline

- Sampling
- Gradient estimation

$$\rho(\mathbf{x} \in \mathbb{R}^2) = \sum_{\mathbf{y} \in D} K\left(\frac{\|\mathbf{x} - \mathbf{y}\|}{p_r}\right)$$

- Advection
- Smoothing

- Iterate  $n$  times until stable layout
  - Predefined 10 or 15 times
  - Automatically determined at runtime?

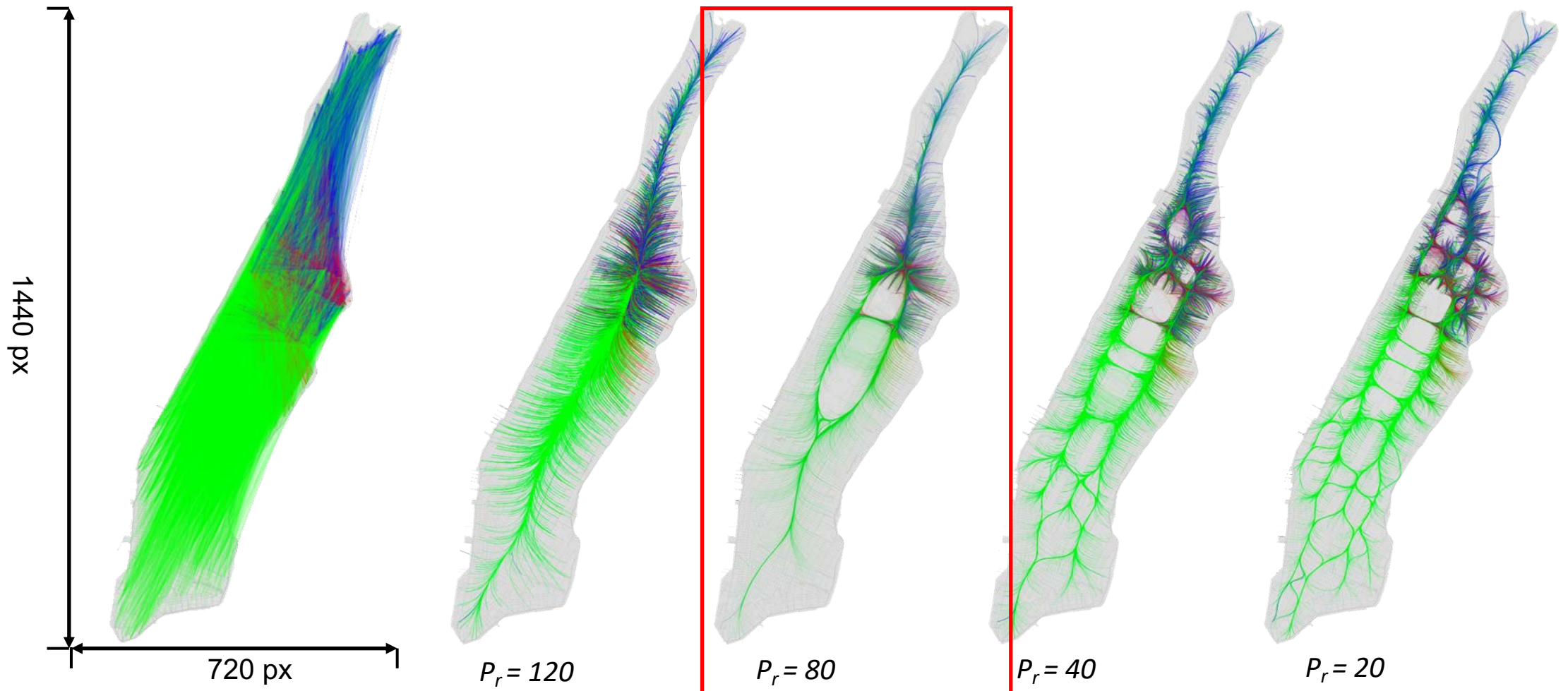




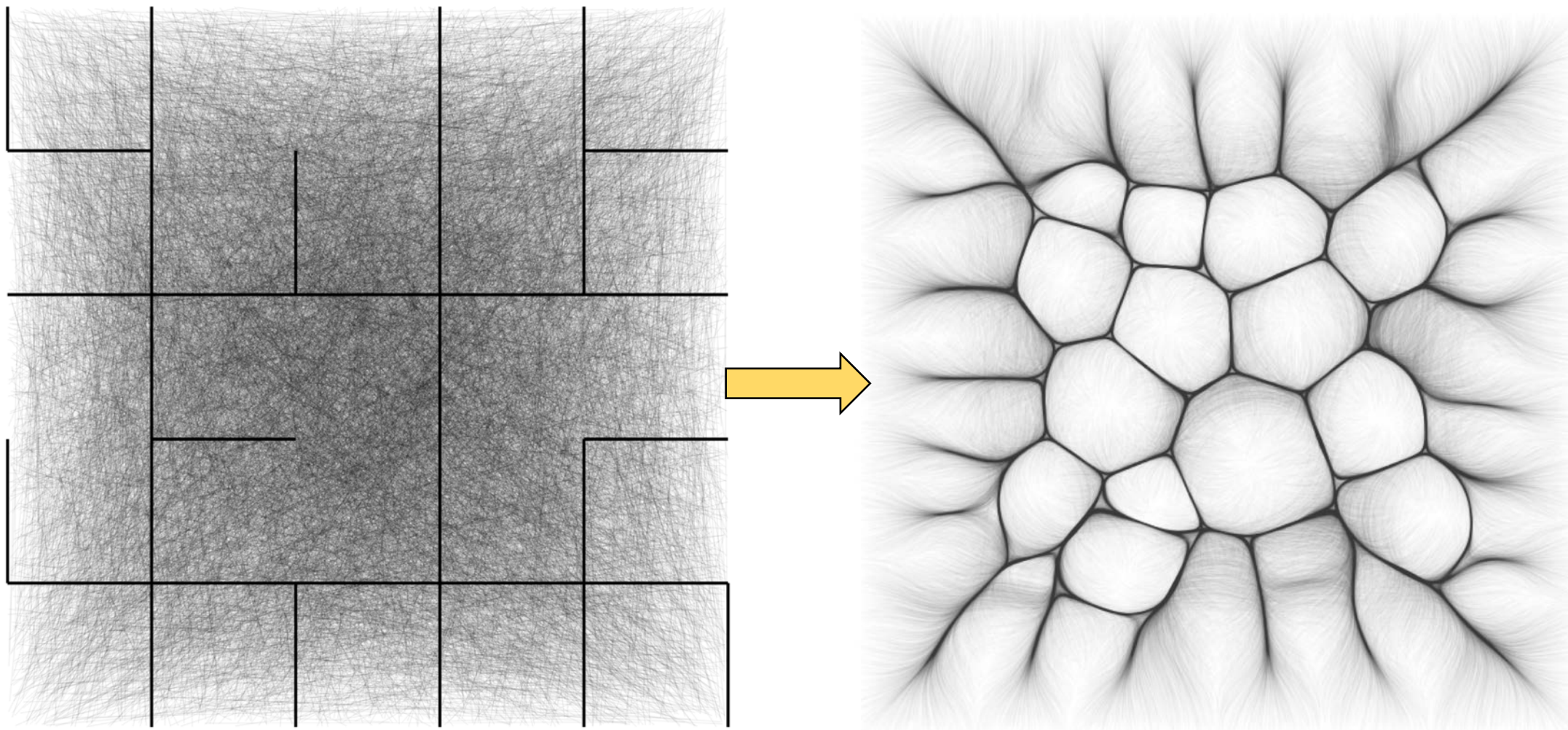
# Limitations of KDEEB: What is a suitable $p_r$ ?

- KDEEB: 5% of graph drawing size

- $5\% \times \sqrt{1440^2 + 720^2} = 80.5$



## Limitations of KDEEB: Road neglect

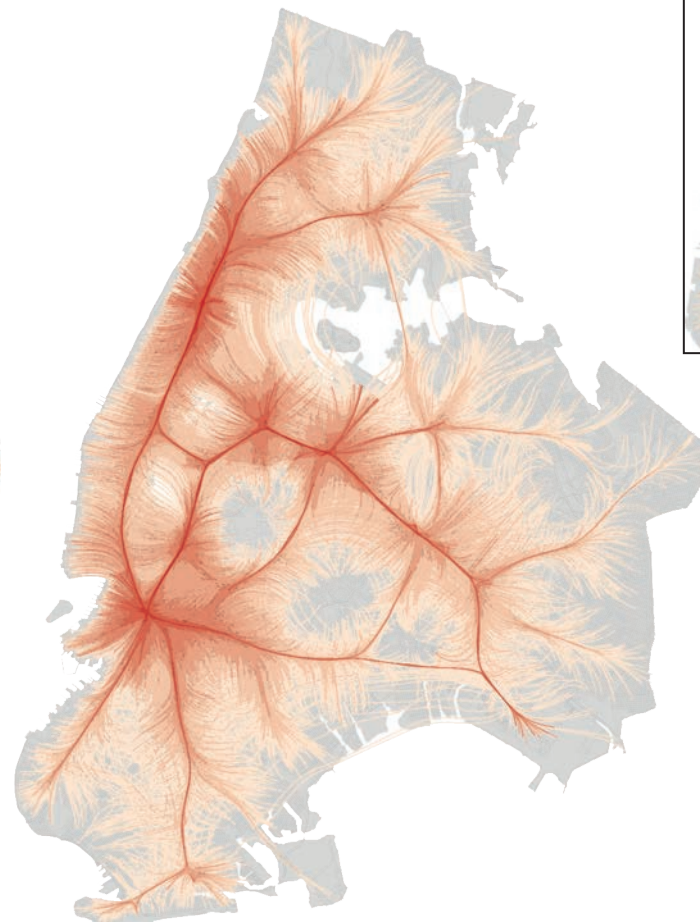




# Limitations of KDEEB



Map Matching



KDEEB ( $p_r = 60$ )



Artifacts

KDEEB ( $p_r = 21$ )

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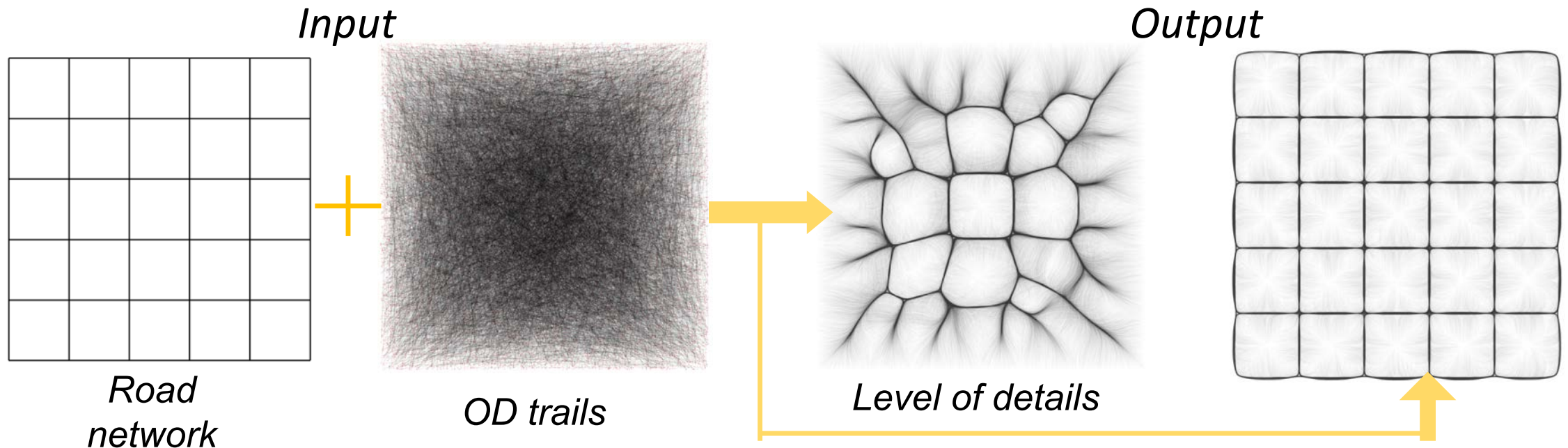
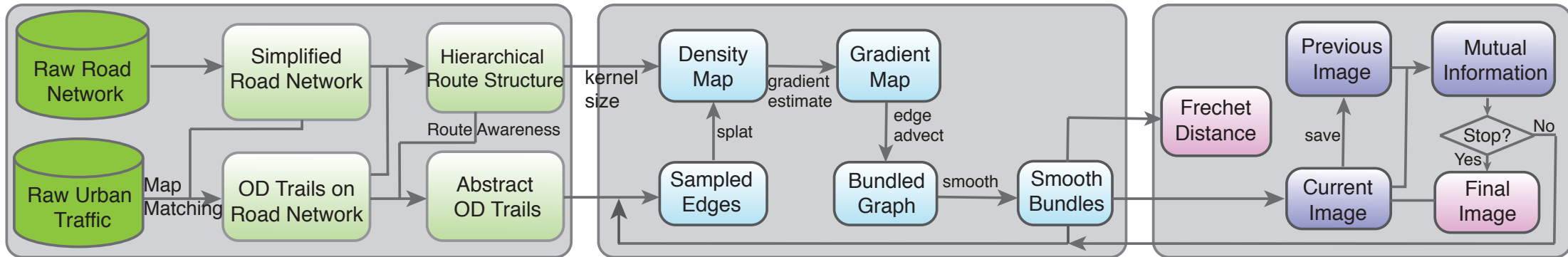
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- Preprocessing:
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  - Bundle termination
  - Bundle deviation

## ■ Conclusion and Future Work

# Route-Aware Edge Bundling

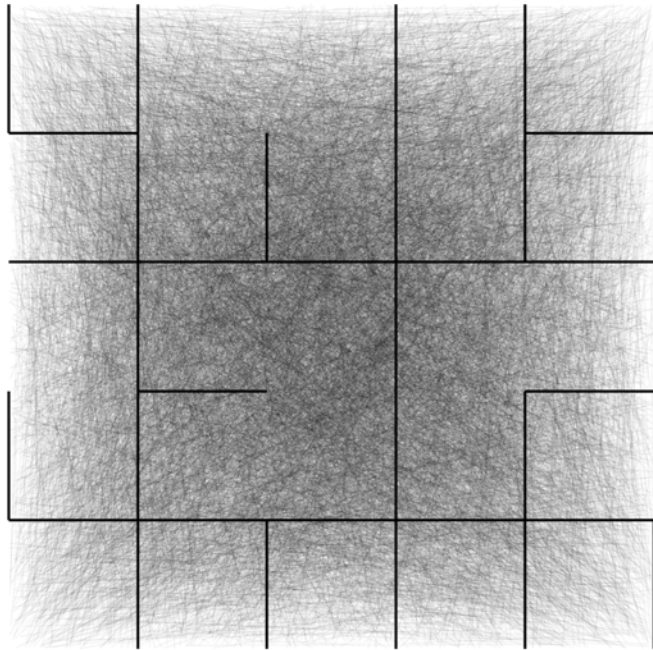
- RAEB pipeline: 1) Preprocessing, 2) Bundling, and 3) Evaluation



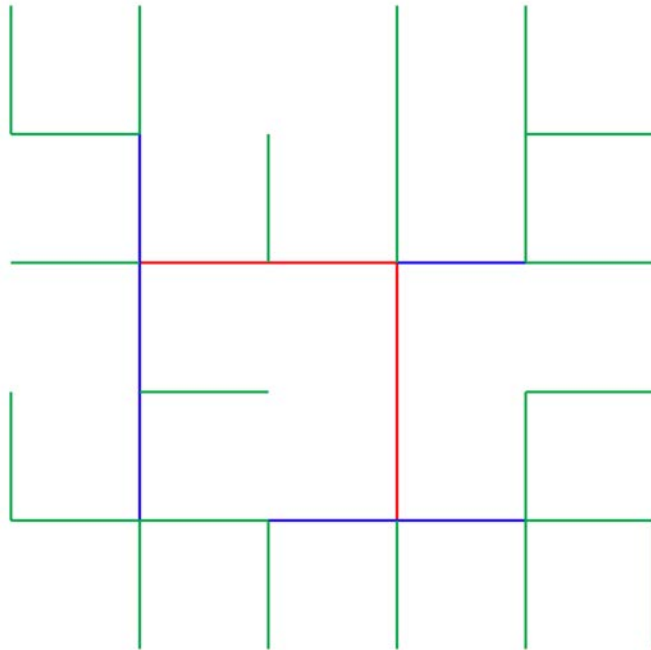


# Preprocessing

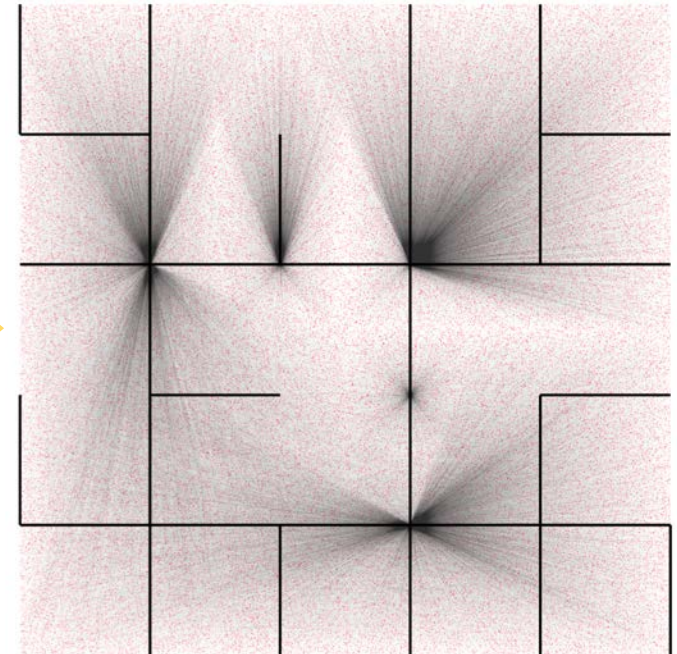
- Build a simplified hierarchical road and traffic network representation.
  - Map matching: shortest path for OD only, ST-matching for GPS traces
  - Hierarchical structure construction: route length, road hierarchy, flow magnitude
  - Trail abstraction: route awareness ( $p_{ra}$ )



*OD Trails &  
Road network*



*Hierarchical  
route structure*



*Trail Abstraction*

# Bundling

- KDEEB applied to the hierarchical structure.
  - Optimal kernel size setting
  - Density map generation

$$\rho_{raeb}(\mathbf{x} \in \mathbb{R}^2) = \sum_{\mathbf{y} \in D} K\left(\frac{\|\mathbf{x} - \mathbf{y}\|}{p_r}\right) + \theta \sum_{\mathbf{r} \in R_{aware}} \Theta(\|\mathbf{x} - \mathbf{r}\|),$$

---

**Algorithm 1** KernelSizeSetting

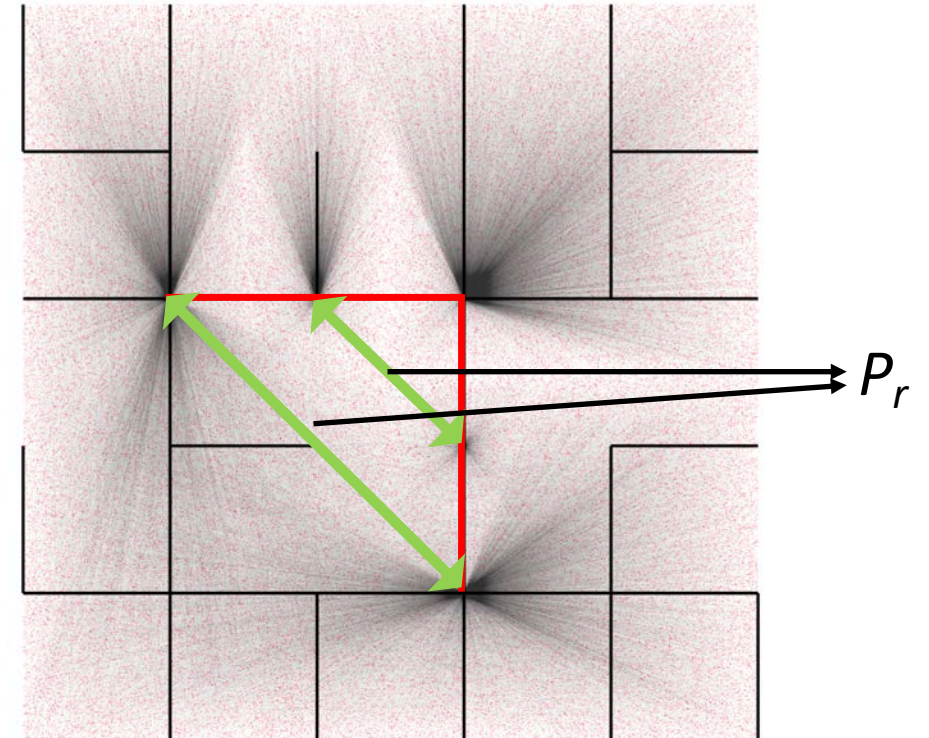
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**Input:** Top  $N$  routes  $P = \{P_1, \dots, P_N\}$

**Output:** Initial kernel size  $p_r$

```
1: for  $i = 1$  to  $N$  do
2:   for  $j = i + 1$  to  $N$  do
3:      $d[i][j] = d[j][i] = \text{DiscreteFrechetDistance}(P_i, P_j)$ 
4:  $C = \text{DBSCAN}(P, \varepsilon, \text{minNum})$ ;
5:  $C_{max} = \text{argmax}_{C_i \in C} |C_i|$ ;
6:  $d_{geo} = 0$ ;
7: for each  $P_i \in C_{max}$  do
8:   for each  $P_j \in C_{max} \ \&\& \ i \neq j$  do
9:      $d_{geo} = d_{geo} + d[i][j]$ ;
10:  $p_r = d_{geo} / |C_{max}| / (|C_{max}| - 1) / 2$ ;
11: return  $p_r$ 
```

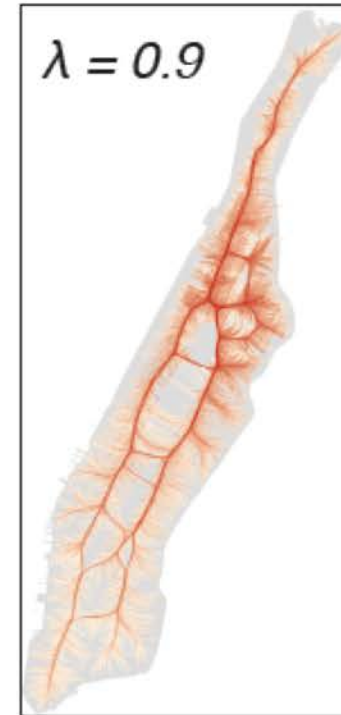
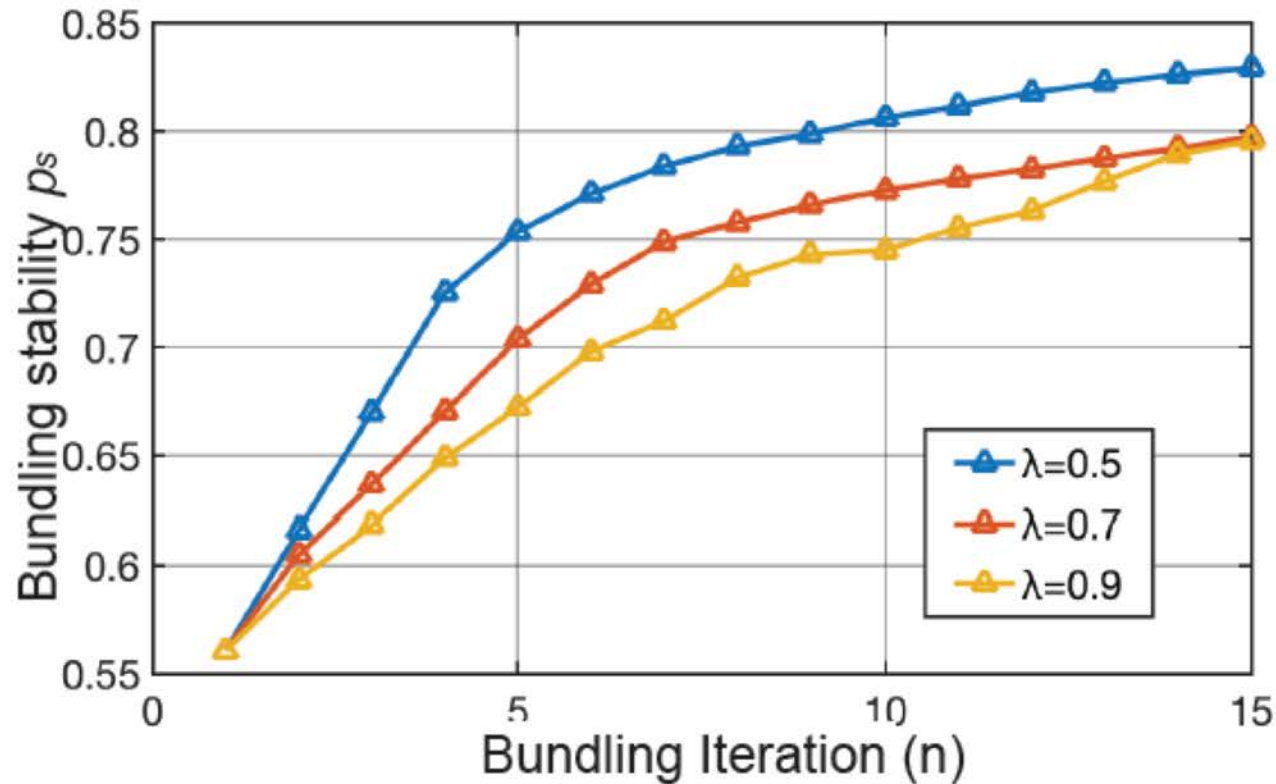
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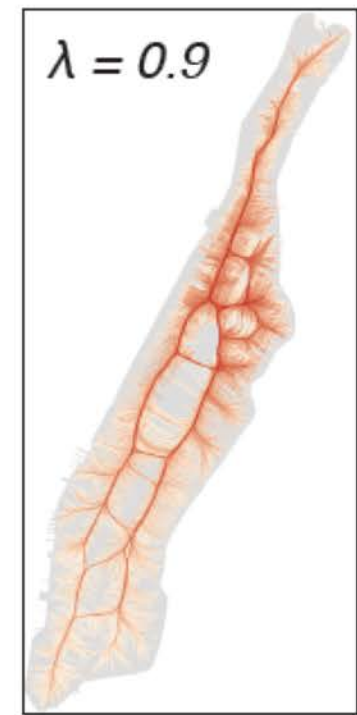
# Evaluation

- Termination: Bundle stability ( $p_s$ ) to determine when to stop iteration

- Bunc 
$$NMI(X,Y) = \frac{2MI(X,Y)}{H(X) + H(Y)} \quad MI(X,Y) = \sum_{x \in X} \sum_{y \in Y} p(x,y) \log \left( \frac{p(x,y)}{p(x)p(y)} \right)$$



$n = 10$



$n = 11$

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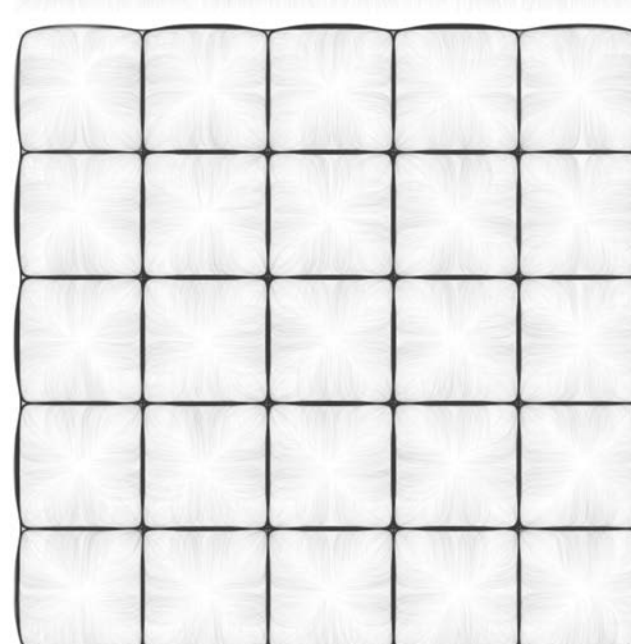
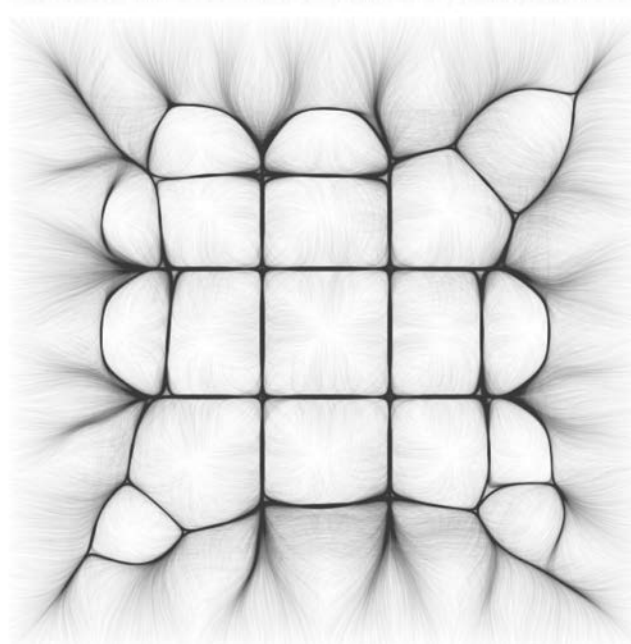
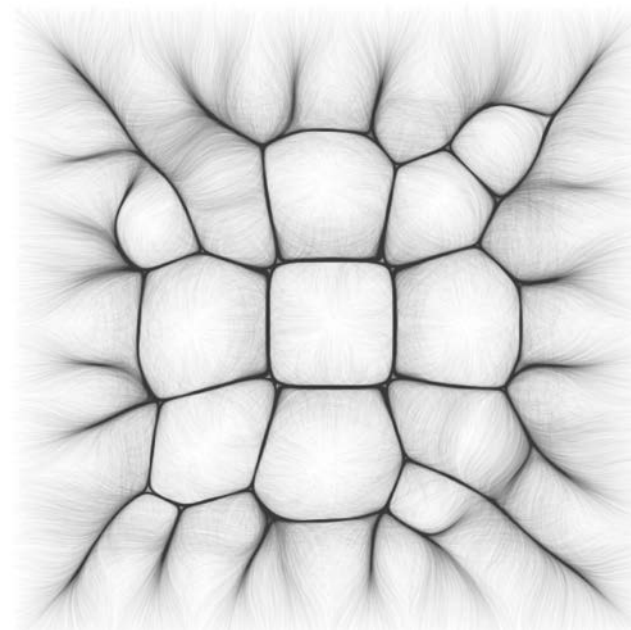
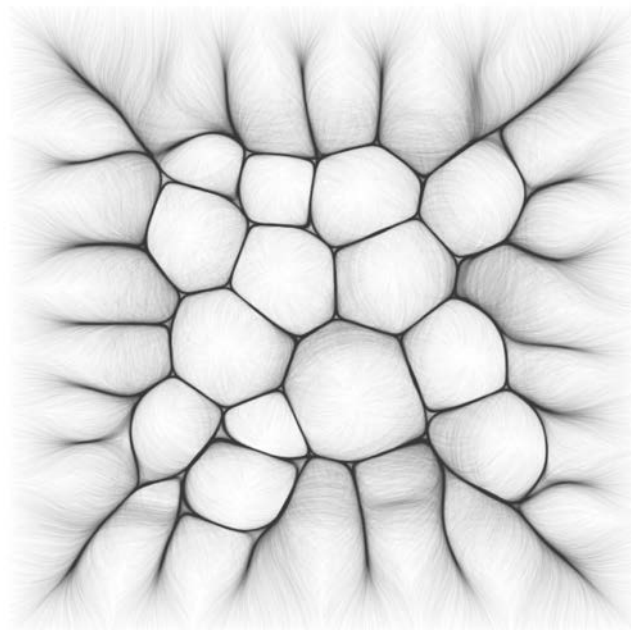
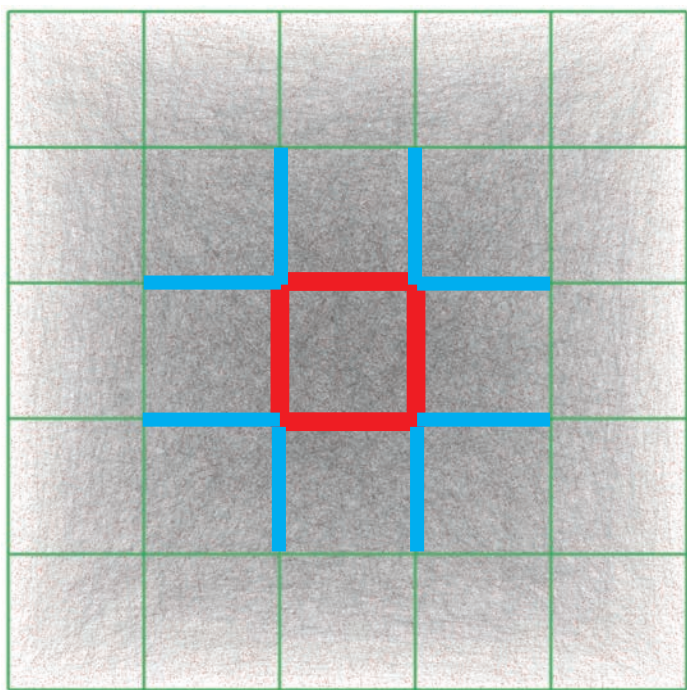
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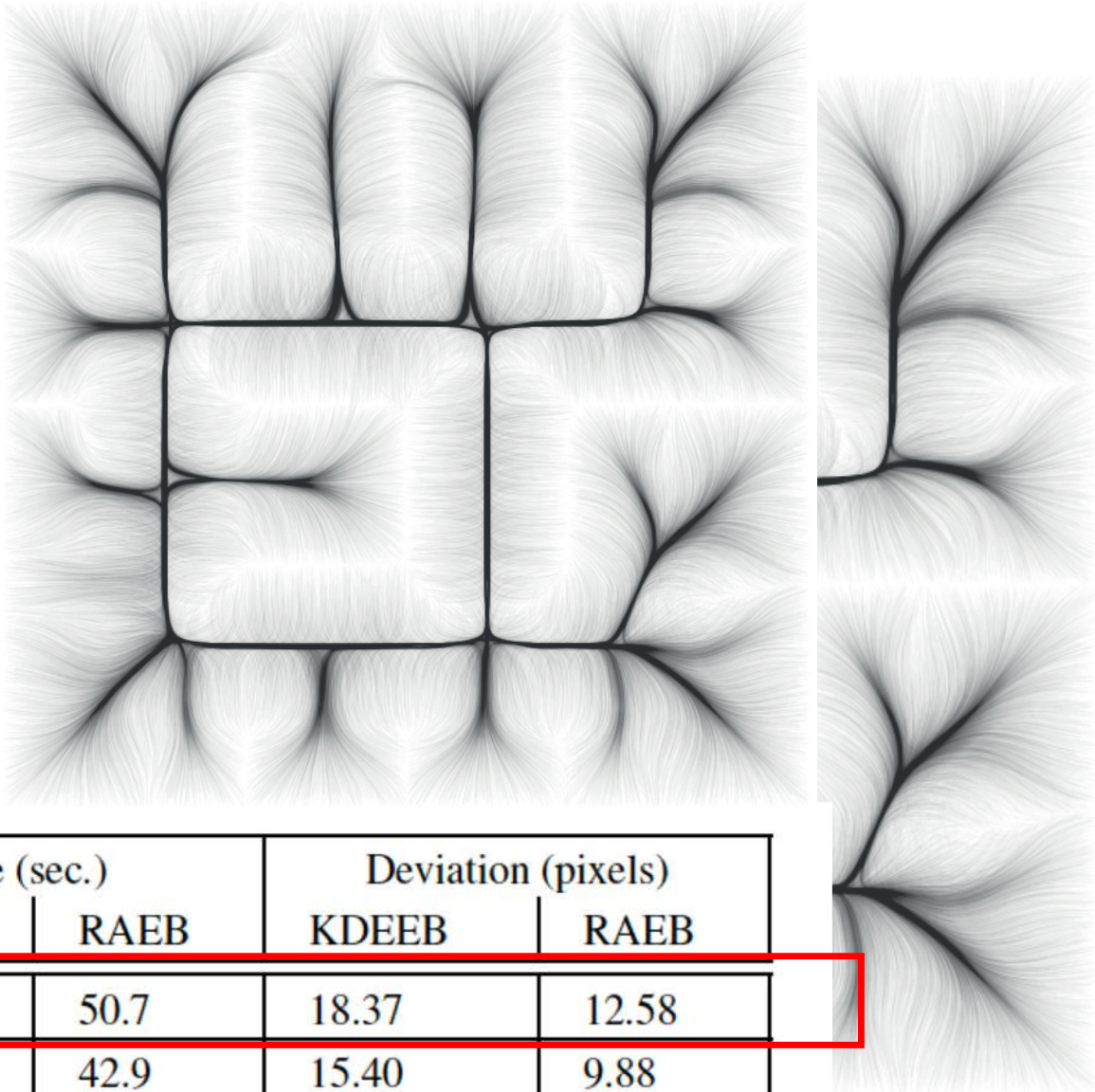
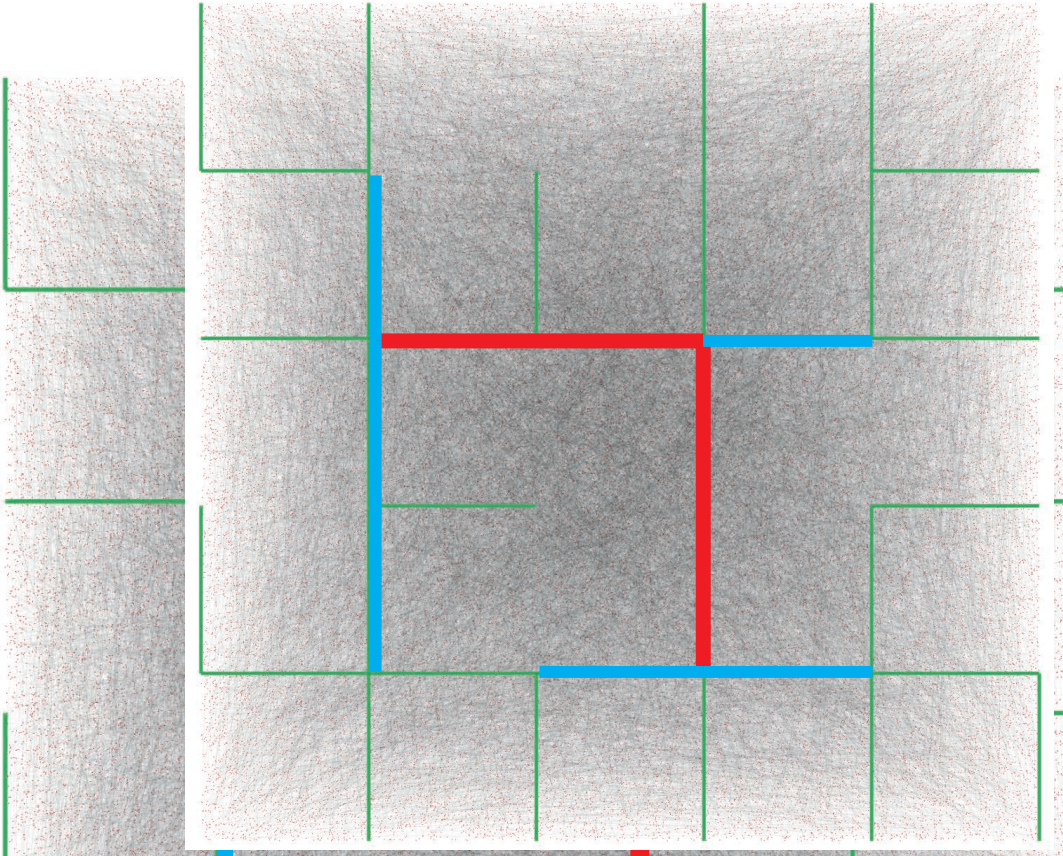


# Application 1: Synthetic Data





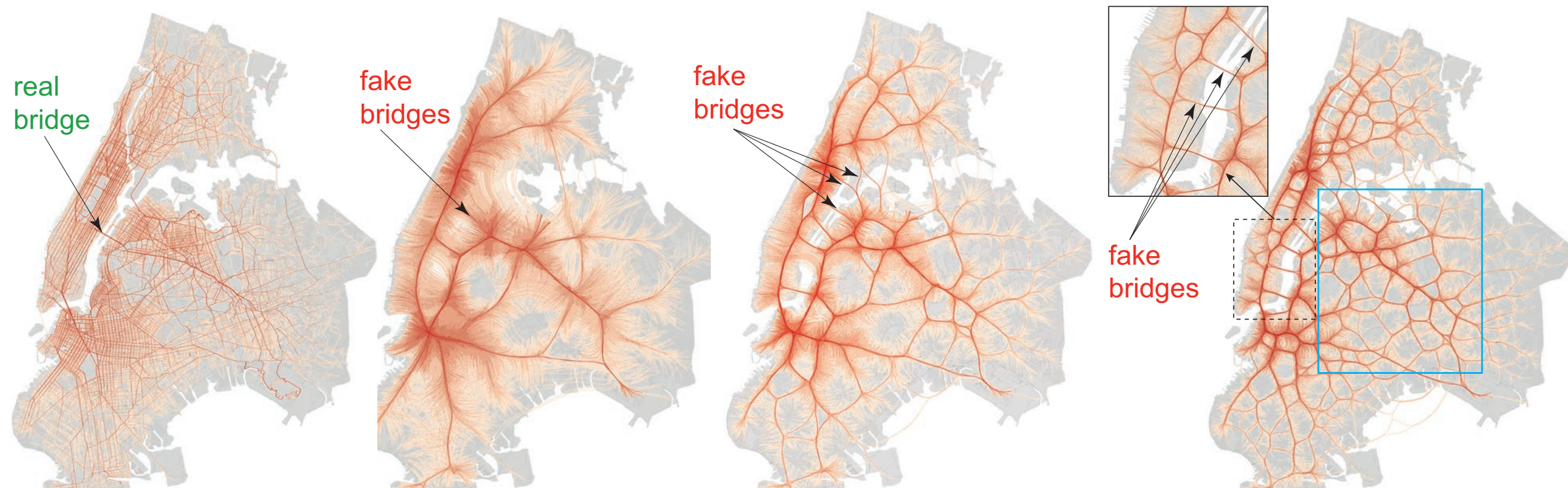
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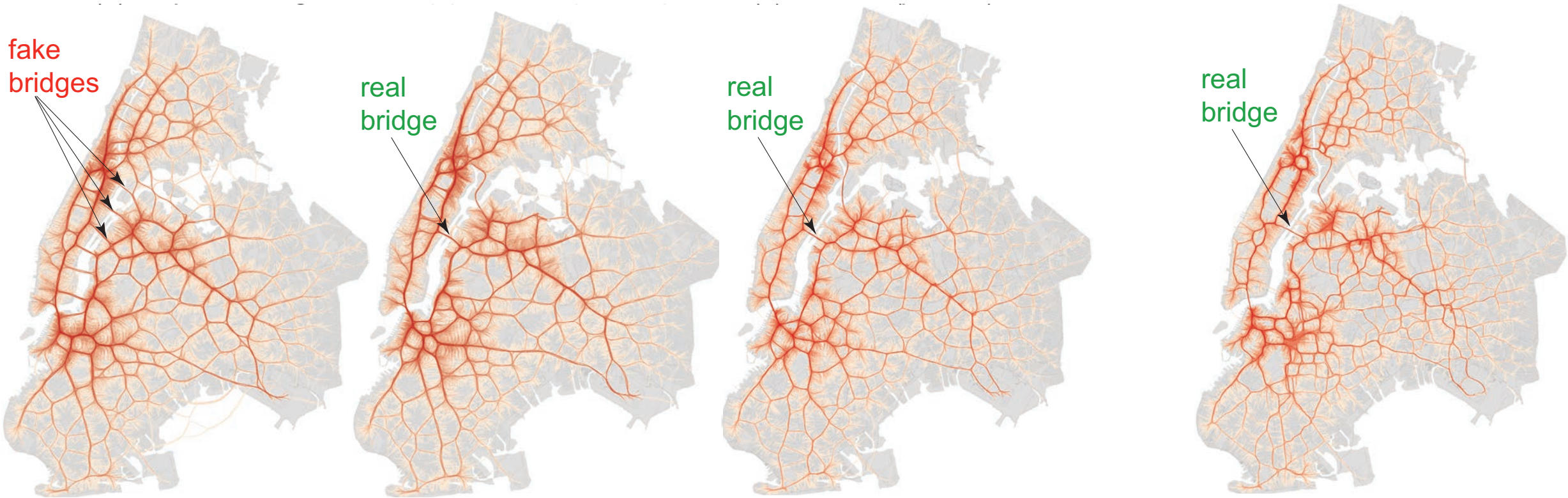
Dataset	Edge samples	$p_n$	Time (sec.)		Deviation (pixels)	
			KDEEB	RAEB	KDEEB	RAEB
Synthetic	4.6M	13	40.3	50.7	18.37	12.58
New York	3.1M	11	34.3	42.9	15.40	9.88
Shenzhen	1.3M	8	13.8	22.8	13.71	10.53



## Application 2: NYC Taxi



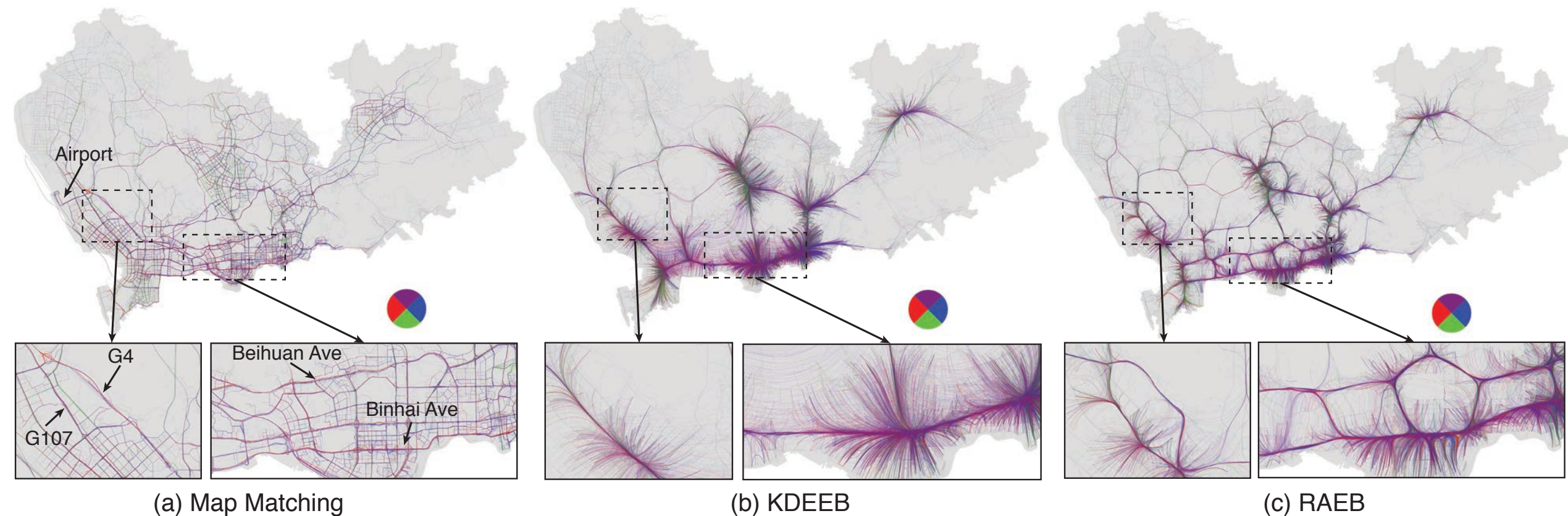
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# Application 3: Shenzhen Taxi



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# Discussions

- RAEB constrains trails to a given road network
  - **Route awareness ( $p_{ra}$ ):** controls how bundles follow roads at a user-selected hierarchy level.
  - **Kernel size ( $p_r$ ):** determined by both the road network geometry and its resolution in image space.
  - **Bundling stability ( $p_s$ ):** automatically stops bundling when this similarity exceeds a given threshold.
- RAEB outperforms KDEEB on both synthetic and real OD trails
  - Visually more realistic
  - Quantitatively closer to ground-truth results
  - Comparable running time
- Limitations and future work
  - Visual hints on bundle deformation
  - Incorporate directional bundling techniques
  - Local and adaptive parameter settings:  $p_{ra}$  and  $p_r$



谢谢！

**Thank You!**

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